

2017 Canadian Computing Olympiad

Day 2, Problem 1

Rainfall Capture

Time Limit: 1 second

Problem Description

It was a dark and stormy night. It also rained, and rained, and rained.

Lucy wants to capture some of the rain, but she only has limited materials. She has a collection of pillars, of various heights, which she can configure to capture the rain. Each pillar is an integer height and has length and width of 1. Once Lucy has her configuration of pillars, she has enough other siding material to enclose the front and back to allow rain to fill the all the available space in between pillars. There is more than enough rain and any excess rain will overflow and get absorbed into the earth.

For example, if Lucy has pillars of height 1, 5, 2, 1, 4, she could configure them as follows (all configurations are illustrated from the side):

```
 *
 *  *
 *  *
 * * *
*****
```

which would capture 5 units of rain (R) as follows:

```
 *
 *RR*
 *RR*
 * *R*
*****
```

For this first collection of pillars (1, 5, 2, 1, 4), she could also capture 6 units of rain as follows:

```
 *
 *RR*
 *RR*
 * *RR*
*****
```

As another example, if the collection of pillars was 5, 1, 5, 1, 5, Lucy could capture 8 units of rain as follows:

```
*R*R*
*R*R*
*R*R*
*R*R*
*****
```

Finally, this configuration of (5, 1, 4, 1, 5) captures 9 units of rain:

```
*RRR*
*R*R*
*R*R*
*R*R*
*****
```

Lucy has N pillars ($2 \leq N \leq 500$) with heights $h_1, h_2 \dots h_N$ ($1 \leq h_i \leq 50$). She would like to know, of all possible configurations of pillars, what are all of the obtainable volumes of rainfall that she can capture using these N pillars.

Input Specification

The first line contains the integer N ($2 \leq N \leq 500$) signifying the number of pillars. The next line contains the integers h_i ($1 \leq h_i \leq 50, 1 \leq i \leq N$), representing the i th pillar height.

For 5 of the 25 marks available, $N \leq 10$.

For an additional 10 of the 25 marks available, $N \leq 50$.

Output Specification

On one line, output a space-separated list of all possible obtainable integer volumes of rain captured, in increasing order.

Sample Input 1

```
5
1 5 2 1 4
```

Output for Sample Input 1

```
0 1 2 3 4 5 6 8
```

Explanation for Output for Sample Input 1

This is the first given example.

Sample Input 2

5
5 1 5 1 5

Output for Sample Input 2

0 4 8

Explanation for Output for Sample Input 2

This is the second given example.

Sample Input 3

5
5 1 4 1 5

Output for Sample Input 3

0 1 3 4 5 6 7 8 9

Explanation for Output for Sample Input 3

This is the third given example.

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Day 2, Problem 2

Professional Network

Time Limit: 2 seconds

Problem Description

Kevin is developing his professional network within a certain community. Unfortunately, he has not connected with anybody yet. But he has his eyes on N potentially valuable connections, numbered from 1 to N . He is determined to connect with them all.

However, few people in this community are willing to friend an outsider. Each of the N people Kevin wants to connect with has similar, but different criteria for determining who is an outsider and who isn't. Person i is willing to friend Kevin if he either has at least A_i connections within the community already, or if Kevin gives this person B_i Internet Points.

Kevin likes his Internet Points very much, and so he doesn't want to give away too many. Now it is your job to help Kevin give away the least number of Internet Points while still making connections with each of the N people.

Input Specification

The first line will contain the integer N ($1 \leq N \leq 200\,000$). Each of the next N lines will contain integers A_i and B_i ($1 \leq i \leq N; 0 \leq A_i \leq N; 0 \leq B_i \leq 10\,000$).

For 2 of the 25 available marks, $B_i = 1$ for all i .

For an additional 4 of the 25 available marks, $N \leq 10$.

For an additional 7 of the 25 available marks, $N \leq 1000$.

Output Specification

Output one integer on a single line, the minimum number of Internet Points Kevin has to give away.

Sample Input 1

```
4
3 3
1 2
0 5
3 4
```

Output for Sample Input 1

```
3
```

Explanation for Output for Sample Input 1

Kevin can connect with person 3 immediately, and with this connection made, he can also connect with person 2. He doesn't have enough connections to connect with person 1 or person 4, so he gives 3 Internet Points to person 1 to acquire 3 total connections which enables him to connect with person 4.

Sample Input 2

```
5
0 9
1 8
2 7
3 6
4 5
```

Output for Sample Input 2

```
0
```

Explanation for Output for Sample Input 2

It is possible that Kevin can connect with everyone without giving away any Internet Points.

Sample Input 3

```
3
0 6
2 7
3 8
```

Output for Sample Input 3

```
8
```

Explanation for Output for Sample Input 3

Kevin should connect with person 1 immediately, then give 8 Internet Points to person 3 to connect with them, then connect with person 2.

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Day 2, Problem 3
Shifty Grid

Time Limit: 2 seconds

Problem Description

You are given a rectangular grid of numbered tiles, with no empty spaces. This grid can only be manipulated using a sequence of *shift* operations. A shift involves either moving an entire row left or right by some number of units, or moving an entire column up or down by some number of units. Tiles which move outside of the rectangular boundaries wrap around to the opposite side of the grid. For example, in the grid

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

a vertical shift downwards by one applied to the second column has the following result:

0	13	2	3
4	1	6	7
8	5	10	11
12	9	14	15

Notice that a left shift by K units is the same as a right shift by $N - K$ units. Similarly, an upward shift by K units is a downward shift by $M - K$ units. Thus, without loss of generality, we will restrict the shift directions to be only to the right or down.

In a grid with N rows and M columns, there are NM tiles in total. You may assume that the tiles are numbered with distinct integers from 0 to $NM - 1$.

You may have noticed that in the first example given above, the tiles are in a very organized formation. We call such arrangements *solved*. That is, a grid of tiles is solved when the first row contains the numbers from 0 to $M - 1$ in order, the second row has the numbers from M to $2M - 1$ in order, and so on, with the last row having the number $(N - 1)M$ to $NM - 1$ in order.

Find a sequence of shift operations that restores a scrambled grid to a solved state.

Input Specification

The first line will contain two space-separated integers N and M ($2 \leq N, M \leq 100$). The next N lines will contain M space-separated integers, representing the grid.

Note that both N and M will always be even, and there will be a solution requiring at most 10^5 shift operations.

For 5 of the available 25 marks, $N \cdot M \leq 8$.

For an additional 10 of the available 25 marks, the puzzle is solvable in at most 2 moves.

Output Specification

Output any sequence of moves that solves the puzzle, in the following format:

- The first line of output should contain a single integer K ($1 \leq K \leq 10^5$), representing the number of moves in the sequence.
- The next K lines should be either of the form $1 \ i \ r$ ($1 \leq i \leq N, 0 \leq r < M$) representing a right shift of the i -th row by r , or of the form $2 \ j \ d$ ($1 \leq j \leq M, 0 \leq d < N$) representing a down shift of the j -th column by d .

Sample Input 1

```
2 4
4 2 3 0
1 5 6 7
```

Output for Sample Input 1

```
2
2 1 1
1 1 1
```

Explanation for Output for Sample Input 1

We shift the first column down by one to obtain

```
1 2 3 0
4 5 6 7
```

then shift the first row right by one to reach the state

```
0 1 2 3
4 5 6 7
```

which is solved.

Sample Input 2

4 2
2 3
5 0
4 1
6 7

Output for Sample Input 2

7
1 1 1
2 1 1
1 2 1
1 3 1
2 1 2
1 1 1
2 1 1

Explanation for Output for Sample Input 2

The sequence of shifts, starting from the input is:

2 3	3 2	6 2	6 2	6 2	1 2	2 1	0 1
5 0	-> 5 0	-> 3 0	-> 0 3	-> 0 3	-> 4 3	-> 4 3	-> 2 3
4 1	4 1	5 1	5 1	1 5	6 5	6 5	4 5
6 7	6 7	4 7	4 7	4 7	0 7	0 7	6 7