Finding a Job

Today we will talk about ways you can go out and make money in today’s economy. The first and most obvious way is going out and finding a paying job. One type of paying job you can find is selling valuable items, or services, and earning commission.

Commission

Commission is when you sell something for a certain amount of $x$ dollars and take a portion of the money made for yourself. This portion is represented by a percentage called the commission rate. Employers offer pay their employees with commission to motivate them to sell more.

Problem 1: You found a job selling boxes of chocolate almonds that pays a commission rate of 20%. The price of a box of chocolate almonds is $4.

1. How much commission do you make selling one box of chocolate almonds?
2. If you sell $100 worth of chocolate almonds, how much commission do you make?

3. If you need to make $200, how many boxes of chocolate almonds must you sell?

Commission With an Hourly Wage

Sometimes, when it’s your job to sell something you are paid an additional hourly wage on top of the commission you make. This is just in case you are not able to sell anything but still need to make money.

Problem 2: You found a new job working at a sports store. The job pays a commission rate of 5% for anything you sell in the store, and an hourly wage of $12 per hour. On your first day you started at 10:00a.m., left for lunch at 1:00p.m., and came back at 2:00pm.

1. In the morning, you sold a pair of goalie pads for $400, two hockey sticks for $250 each, and a football for $20. How much money did you earn before you went to lunch?
2. After lunch, you worked for 4 more hours and sold a basketball net for $300 and two tennis rackets for $60 each. How much money have you earned so far?

3. Your shift is ending at 7:00p.m. and you have one more customer who has scheduled an appointment within that time to purchase a pair of roller skates. If your goal is to have made $170 at the end of your shift, how much money must you sell the roller skates for?

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**Graduated Commission**

Another way your employers encourage you to sell more is by offering graduated commission—once you sell a certain amount of items, or services, the commission rate increases for every sale after that, giving you more commission per sale.
Problem 3: You find a job making Rubik’s Cubes at Rubik’s Factory. You get paid $13 an hour and $1 for the first 15 cubes you make, $2 for the next 10, and $3 for any cubes after that. It takes you 15 minutes to make one Rubik’s Cube.

1. How much money do you make if you work for 8 hours at Rubik’s Factory?

2. After the first week, Rubik changes your shift to only 5 hours. However, you want to earn the same amount of money as you did working for 8 hours. How many cubes must you make per hour?

3. Rubik changes your shift back to 8 hours, except now he pays you the same commission rate regardless of how many cubes you make. If he promises to pay you $225 for the whole shift and you make 9 cubes per hour, what is the new commission rate?
Earning Interest

Once you have found a job and earned some money, you can then invest that money to earn even more by receiving interest. What’s meant by “investing and receiving interest”, is just lending someone a certain amount of money who then pays you back that same amount plus a little extra (the interest) for the favour you did them. The interest will always be a percentage of the amount of money you invested, a percentage called the interest rate. The first type of interest we’ll discuss is simple interest.

Simple Interest

Under simple interest, the interest earned is calculated by multiplying the original amount invested, called the principal, by the yearly interest rate, which is multiplied by the length of the investment in years.

The formula to calculate simple interest, $I$, is

$$I = P \times r \times t$$

Where $P$ is the principal amount (or original amount) invested, $r$ is the yearly interest rate, and $t$ is the time in years.

Example: You invest $100 at the local bank that pays simple interest at the end of the year at an interest rate of 5%.

1. How much interest have you earned at the end of the year? How much money do you have now?

$$I = ?$$

$$P =$$

$$r =$$

$$t =$$
Accumulated Value

The accumulated value of an investment, $A$, is the amount of money you invested plus the interest you earned. So the accumulated value of an investment under simple interest is

\[ A = P + P \cdot r \cdot t \]

Where, again, $P$ is the principal amount invested, $r$ is the yearly interest rate, and $t$ is the time in years.

Problem 4: You earned $200 in October and now want to invest your money. You find an owner of a lemonade stand in need of some lemons, so offer to buy them $200 worth of lemons.

1. If you charge simple interest at a yearly rate of 10%, how much money will you have accumulated in 6 months?
   \[
   A = ? \\
   P = \\
   r = \\
   t = 
   \]

2. The owner of the lemonade stand says that $200 worth of lemons is too much. Instead, they tell you that they will pay you back $200 in total at the end of one year at a yearly interest rate of 15%. How many dollars worth of lemons must you buy for the owner of the lemonade stand?
   \[
   P = ? \\
   A = \\
   r = \\
   t = 
   \]
3. How long would it take, in years, for the owner of lemonade stand to pay you back $180 if you bought them $150 worth of lemons at an interest rate of 10%?

\[ t = ? \]

\[ P = \]

\[ A = \]

\[ r = \]

**Compound Interest**

Under compound interest, the interest earned is calculated by multiplying the principal amount and the interest already earned by the yearly interest rate.

**Example:** Assume that you have deposited $1000 into a savings account that pays 10% compounded annually

After one year, the money earns __________________. The new balance is then ________.

After two years, the money earns __________________. The new balance is then ________.

After three years, the money earns __________________. The new balance is then ________.

And so on.

Under compound interest, the formula to calculate the accumulated value, \( A \), is

Where \( P \) is the principal amount, \( r \) is the annually compounded interest rate, and \( t \) is the time in years.
Problem 5: You open up a savings account that pays 4% compounded annually.

1. If you deposit $100, how much money will you save in 3 years?

\[
\begin{align*}
A &= ? \\
P &= 100 \\
r &= 0.04 \\
t &= 3
\end{align*}
\]

2. If in 6 years you will have saved $2530.64, how much money did you deposit?

\[
\begin{align*}
P &= ? \\
A &= 2530.64 \\
r &= 0.04 \\
t &= 6
\end{align*}
\]

3. What would the interest rate have changed to if you saved $1650 with an initial deposit of $1500 two years ago.

\[
\begin{align*}
r &= ? \\
P &= 1500 \\
A &= 1650 \\
t &= 2
\end{align*}
\]
Problem Set

"*" indicates challenge question

1. You find a job selling water that pays a 10% commission rate on the sales you make. If you sold $150 worth of water in a week, how much commission did you make that week?

2. You invest $50 into a savings account at the local bank that pays simple interest at an interest rate of 5% per year. How much interest have you earned in 10 months?

3. You find a job painting garages that pays an hourly wage of $12 per hour and a commission rate of 7%. If the company you work for charges $50 for every garage they paint, how much money did you make your first day if you painted 3 garages in 5 hours?

4. You lend $500 to a start-up clothing company called “RVS” and demand that they pay you back in 2 years at an interest rate of 20% per year compounded annually. How much will “RVS” pay you in full at the end of 2?

5. You find a job cutting hair that pays you with graduated commission. You make $10 for your first 2 haircuts, $12 for your next 3, and $14 for any amount after that in any given day of work. How many haircuts must you provide to make $126 in one day?

6. From the problem above- your employer takes away the graduated commission and pays you with one commission rate regardless of how many haircuts you provide. If he promises to still pay you $126 for the same amount of haircuts, what is the new commission rate?

7. A friend that you lent money to one month ago has paid you back $60 in full. If you originally charged them with simple interest at an interest rate of 84% per year, what was the original amount you lent them?

8. You see an advertisement in the newspaper that two different employers are hiring for the same job of selling skis. One employer pays 15$ per hour and the other pays 5% commission for your sales. How many dollars worth of skis must you sell in an hour so that both jobs are just as good?

9. * Prove that for any investment, $P$, that pays an annual interest rate, $r$, and lasts exactly 1 year, that the accumulated value is the same under simple and compound interest.
10. * You are trying to decide which student you should teach to skate. Kayla pays you $30 to show up and $15 per hour for each lesson. Raheem pays you $20 per hour for each lesson. How many hours do both lessons need to be so that teaching both students is just as good?

11. * You wish to accumulate $250 with an investment of $200 over 3 years. What interest rate compounded annually must you ask for? Round to the nearest thousandth.

12. * There are two investment options:
   
   (a) Invest $100 at an interest rate $r$ compounded annually over 4 years.
   
   (b) Invest $50 at an interest rate $r$ compounded annually over 8 years.

   Solve for the interest rate $r$ compounded annually such that these two investment options accumulate to the same value. Round to the nearest thousandth.

13. * One summer you worked as a sales person selling laptops. The job paid you $22 per hour and a commission rate $c$. You invested all of the money you made working that summer into a savings account that offered an interest rate of 10% compounded annually. After 3 years your savings account has accumulated $13310. If you worked 40 hours per week for 8 weeks and sold $11840 worth of laptops that summer, 3 years ago, what was the commission rate of your job selling laptops.

14. * You lent a certain amount of money to a start-up chocolate bar company. To repay you, the company pays you $10 after the first year, $20 dollars after the second year, and repeats this payment process of paying 10 more dollars each year for 50 years (10, 20, 30, 40...). They tell you that this will be the total amount of interest you earn for lending them money. If the yearly simple interest rate was 5% when you made the agreement to lend them money, how much money did you lend them.